

## Generalized Instrumental Variables Estimation of Nonlinear Rational Expectations Models

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Econometrica, Volume 52, Issue 1 (Jan., 1984), 267-268.

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## **ERRATA**

IN T. B. FOMBY AND R. C. HILL, "Multicollinearity and the Minimax Conditions of the Bock Stein-Like Estimator," *Econometrica*, 47(1979), 211–212, the expression in the second line from the bottom of p. 211,

$$[2 + \rho^2 \pm \rho(\rho^2 + 8)^{1/2}] \div [2(1 - \rho^2)],$$

should read

$$2 \div \left[2 + \rho^2 \pm \rho(\rho^2 + 8)^{1/2}\right].$$

The remaining contents are not affected, including the reported numerical results.

The authors would like to thank Mr. Subarna Samanta for bringing this error to their attention.

\* \* \*

An error has been pointed out by Patrick Sevestre in the recent paper by S. J. Nickell, "Biases in Dynamic Models with Fixed Effects," *Econometrica*, 49(1981), 1417–1426. On page 1424 it is noted that the small T bias in the coefficient on the lagged dependent variable in a fixed effects model is larger if exogenous variables are included. This statement is incorrect. The following is, however, true. If the true model contains exogenous regressors and these are omitted, the "Hurwicz bias" on the lagged dependent variable coefficient becomes smaller. There will, however, also be omitted variable bias which can go either way and applies even when  $T \rightarrow \infty$ . The remark in the paper therefore refers only to the Hurwicz bias and this was not made clear.

\* \* \*

DUE TO AN ERROR in the monthly consumption series, the empirical results reported in the paper by Lars Peter Hansen and Kenneth J. Singleton, "Generalized Instrumental Variables Estimation of Nonlinear Rational Expectations Models," *Econometrica*, 50(1982), 1269–1286, are incorrect. Here the authors provide correct versions of Tables I and III. The correct version of Table II is presented in L. P. Hansen and K. J. Singleton, "Stochastic Consumption, Risk Aversion, and the Temporal Behavior of Asset Returns," *Journal of Political Economy*, 91(1983), 249–265.

The correction in the data has an important impact on the estimates of the coefficient of relative risk aversion,  $\alpha$ , and the associated standard errors. For instance, the estimates of  $\alpha$  reported in the revised version of Table I fluctuate considerably more across alternative measures of consumption (nondurables versus nondurables plus services) and across alternative sets of instruments used in estimation. Whereas previously estimates of  $\alpha$  ranged from -.96 to -.68, now they range from -1.59 to 1.26. Values of  $\alpha$  greater than zero imply nonconcave preferences. In addition, the estimated standard errors are considerably higher in the revised version of Table I. In all cases in which the estimate of  $\alpha$  exceeds zero, the estimated standard error is in turn greater than the estimate of  $\alpha$ . Similar observations apply to Table III.

In the revised version of Table III, we have included results obtained using observations on the value-weighted aggregate stock return and the nominal, risk-free bond return. These results are the instrumental variables counterparts to the maximum likelihood results reported in Table 5 of the 1983 JPE article by Hansen and Singleton. Since the nominal risk-free return at time t+1,  $R_{l+1}^f$ , is known at time t, we use  $R_{l+1}^f/R_l^f$  and NLAG lags of this ratio as instruments in place of NLAG lags of the ex post real return on the bound.

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TABLE I
Instrumental Variable Estimates for the Period 1959:2–1978:12

Cons	Return	NLAG	â	SE(α̂)	β̂	SÊ(β̂)	x <sup>2</sup>	DF	Prob
NDS	EWR	1	- 0.9360	2.5550	.9930	.0060	5.226	1	.9774
NDS	<b>EWR</b>	2	0.1529	2.3468	.9906	.0056	7.378	3	.9392
NDS	<b>EWR</b>	4	1.2605	2.2669	.9891	.0059	9.146	7	.7577
NDS	<b>EWR</b>	6	0.1209	2.0455	.9928	.0054	14.556	11	.7963
NDS	VWR	1	-1.0350	1.8765	.9982	.0045	1.071	1	.6993
NDS	VWR	2	0.1426	1.7002	.9965	.0044	3.467	3	.6749
NDS	VWR	4	-0.0210	1.6525	.9969	.0043	5.718	7	.4270
NDS	VWR	6	- 1.1643	1.5104	.9997	.0041	11.040	11	.5601
ND	<b>EWR</b>	1	- 1.5906	1.0941	.9930	.0034	7.186	1	.9926
ND	<b>EWR</b>	2	-0.7127	0.9916	.9918	.0034	12.040	3	.9928
ND	<b>EWR</b>	4	-0.1261	0.8917	.9921	.0035	14.638	7	.9591
ND	<b>EWR</b>	6	-0.4193	0.8256	.9936	.0033	18.016	11	.9188
ND	VWR	1	-1.2028	0.7789	.9976	.0027	1.457	1	.7726
ND	VWR	2	-0.5761	0.7067	.9975	.0027	5.819	3	.8792
ND	VWR	4	-0.6565	0.6896	.9978	.0027	7.923	7	.6606
ND	VWR	6	-0.9638	0.6425	.9985	.0027	10.522	11	.5159

TABLE III
Instrumental Variables Estimation with Multiple Returns

,	INSTR	OMENTAL VARI	ABLES ESTIN	AATION WI	111 14101111	EE KETOKIK	,	
<del>  </del>		Equally- and Val	ue-Weighted /	Aggregate Re	turns 1959:2	-1978:12		
Cons	NLAG	â	$\widehat{SE}(\hat{\alpha})$	β̂	$\widehat{SE}(\hat{\beta})$	$\chi^2$	DF	Prob.
NDS	1	- 0.5901	1.7331	.9989	.0041	18.309	6	.9945
NDS	2	1.0945	1.4907	.9961	.0040	24.412	12	.9821
NDS	4	0.3835	1.4208	.9975	.0039	40.234	24	.9798
ND	1	-0.6494	0.6838	.9982	.0025	19.976	6	.9972
ND	2	-0.0200	0.6071	.9982	.0025	27.089	12	.9925
ND	4	-0.1793	0.5928	.9986	.0025	42.005	24	.9871
111-111	Value-Weig	hted Aggregate S	tock Returns a	ind Risk-Fre	e Bonds Reti	ırns 1959:2-1	978:12	
Cons	NLAG	â	$\widehat{SE}(\hat{\alpha})$	β̂	$\widehat{SE}(\hat{\beta})$	$\chi^2$	DF	Prob.
NDS	1	1405	.0420	.9998	.0001	31.800	8	.9999
NDS	2	1472	.0376	.9998	.0001	44.083	16	.9998
NDS	4	1405	.0320	.9996	.0001	65.250	32	.9995
ND	1	0962	.0461	.9995	.0001	25.623	8	.9988
ND	2	1150	.0377	.9995	.0001	39.874	16	.9991
ND	4	1611	.0364	.9994	.0001	60.846	32	.9985
11,7,70		Three Indus	try-Average S	tock Returns	1959:2-197	7:12		
Cons	NLAG	â	$\widehat{SE}(\hat{\alpha})$	$\hat{oldsymbol{eta}}$	$\widehat{SE}(\hat{\beta})$	$\chi^2$	DF	Prob.
NDS	1	1.5517	1.8006	.9906	.0046	13.840	13	.6147
NDS	4	0.6713	1.2466	.9940	.0035	88.211	49	.9995
ND	1	0.7555	0.7899	.9924	.0029	13.580	13	.5959

0.5312

0.5512

.9939

.0024

49

89.501

.9996